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# Medium-range imperfect order determining the slow β-relaxation in metallic glasses

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Secondary (slow  $\beta$ ) relaxation and structural ABSTRACT heterogeneity are crucial in several critical unresolved issues in metallic glasses (MGs). However, their intrinsic correlations and composition dependence are not established despite extensive work for decades. In this work, we modulated the secondary relaxation and structural heterogeneity of Dy-based bulk MGs by microalloving different metalloids (B, C, N, and Si) and demonstrated the atomic-scale mechanism. We shed light on the effects of enthalpy of mixing, degree of elastic heterogeneity on the micrometer scale, intensity of interaction, and imperfect orders (IPOs) on  $\beta$ -relaxation dynamics. We revealed that both the obviousness/intensity of the shoulder and the activation energy for β-relaxation are closely associated with the fraction of medium-range IPO. This shows that the cooperative string-like atomic rearrangements considered as the structural origin in terms of the first-order transition theory probably occur in soft medium-range structures (or defects) with IPO. In addition, the intensity of interaction between Dy and metalloid elements is found to play a crucial role in the formation of medium-range IPO. This work offers new insights into the longstanding mystery regarding the atomic mechanism of  $\beta$ -relaxation and shows significance for tuning the properties of MGs.

Keywords:  $\beta$ -relaxation, structural heterogeneity, metallic glass, imperfect order

#### **INTRODUCTION**

Glass is one of the most important materials that has promoted the development of modern civilization. Although glass has been used by mankind for millennia, its glassy structure and relaxation dynamics remain longstanding challenges in condensed matter physics and materials science [1–4], which originate from its complex structural and dynamic heterogeneity. Metallic glasses (MGs), which are relatively simple among different kinds of glasses, have a metallic bonding nature and lack of angle jump and intramolecular degree of freedom, which endows them with many unique and outstanding properties and makes them ideal systems for exploring the fundamental physical mechanism of glass formation and relaxation dynamics on the atomic scale [5–8].

Prepared by quenching metallic melts through the glass transition, MGs have no long-range order but considerable diversity in short- to medium-range orders [5-7]. MGs exhibit relaxation dynamics over a wide range of timescales, including  $\alpha$ -relaxation,  $\beta$ -relaxation,  $\gamma$ -relaxation, and boson peak dynamics [9-14]. On this subject, slow  $\beta$ -relaxation (Johari-Goldstein  $\beta$ -relaxation) [15,16], intrinsic to almost all kinds of glasses, is of particular significance because it serves as the precursor of a-relaxation and correlates with many fundamental issues in glassy/liquid physics, such as diffusion, physical aging, crystallization, and fragile-to-strong dynamical transition of liquid [9,16–19]. Furthermore, it has been found that  $\beta$ -relaxation and shear transformation zones have almost the same activation energy, demonstrating a common structural origin [20]. Experimentally, the correlation between  $\beta$ -relaxation and the fraction of liquid-like zones and the distribution of flow units have also been reported [14,15,21,22]. Generally, a correlation between β-relaxation and nanoscale spatial heterogeneity exists [23,24]. Despite the intrinsic feature of spatial heterogeneity of MGs, it is not fully understood with sufficient atomic structural details why distinct relaxation behaviors with pronounced peaks, shoulders, or excess wings are observed in different systems [25-27]. Theoretically, the microscopic origin of β-relaxation remains under intense debate even in MGs [2,28-32].

In this work, rather than exploring a series of MGs with significant composition differences, minor additions ( $\leq 1$  at%) are employed to tune the spatial heterogeneity and  $\beta$ -relaxation, which can considerably simplify the exploration of the composition effect (where the content effect can be largely ignored). By dynamic mechanical, nanoindentation, and structural tests, we intend to shed new light on the following unexplored or not fully comprehended questions: What are the effects of minute changes in composition on the elastic and structural heterogeneity of MGs on different length scales? How does structural heterogeneity correlate with  $\beta$ -relaxation? What type of struc-

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tural motif presents cooperative string-like excitation (in the random first-order transition theory) and thus determines the intensity and activation energy of  $\beta$ -relaxation?

#### MATERIALS AND METHODS

#### Sample preparation

Master alloys were synthesized by arc-melting a mixture of raw metals under a Ti-gathered high-purity argon atmosphere. Each ingot was melted five times to ensure chemical homogeneity. The purity of the Dy element is higher than 99.9%, and those of Al, Co, and metalloid elements (B, C, and Si) are no less than 99.99%. The N element introduction was conducted by arc-melting the AlN compound (purity > 99.99%). Bulk metallic glass (BMG) samples were fabricated by copper mold casting.

#### XRD and TEM

The amorphous structure of the BMGs was studied by X-ray diffraction (XRD) and high-resolution transmission electron microscopy TEM (HRTEM). Samples for TEM studies were prepared by mechanical polishing and ion milling (PIPS 691, Gatan) at 3.0 keV and cooled with liquid nitrogen.

#### **DSC** experiments

Differential scanning calorimetry (DSC, NETZSCH 404 F3) experiments were conducted at a heating rate of 20 K min<sup>-1</sup> to determine the glass transition temperature ( $T_g$ ) and crystallization temperature ( $T_x$ ).

#### Nanoindentation

Nanoindentation tests were carried out using a Hysitron TI 980 TriboIndenter with a standard Berkovich diamond indenter. For the mapping experiment, a loading rate of 100 mN s<sup>-1</sup> was used, and the maximum load was 10 mN. For each sample,  $14 \times 14$  points were measured for the distribution analysis of the reduced modulus and elastic heterogeneity. Creep measurements were performed by loading the sample at a loading rate of 30 mN s<sup>-1</sup> to a maximum load of 50 mN, then a holding period of 180 s, and finally unloaded at 30 mN s<sup>-1</sup>. Six independent measurements were ments were conducted for each sample.

#### **DMA** experiments

The specimens cut from cylindrical BMG samples were mechanically polished mirror-like on one side before nanoindentation measurement. Relaxation behaviors were characterized by dynamical mechanical analysis (DMA, TA 850) with a constant heating rate of 2 K min<sup>-1</sup> at driving frequencies of 1, 2, 5, and 10 Hz. Rectangular specimens with dimensions of 30 mm (length)  $\times$  2 mm (width)  $\times$  1 mm (thickness) were gripped to an oscillating system and subjected to sinusoidal single cantileverbending strains with a limited amplitude of 15 µm.

#### **RESULTS AND DISCUSSION**

The Dy-based BMGs were selected as the model system because they have well-resolved  $\beta$ -relaxation peaks or shoulders and good glass-forming ability (GFA) [14]. The minor addition of metalloid elements B, C, N, and Si, with smaller atomic radii (compared with that of Dy) and a large negative enthalpy of mixing with Dy (shown in Fig. 1a) was adopted to tune the structural heterogeneity and relaxation behavior. Based on the coupling model, strong interactions originating from this large negative enthalpy are beneficial for pronounced  $\beta$ -relaxation [33]. A large negative enthalpy is also favorable for glass formation [14]. The prepared BMGs, Dy<sub>55</sub>Co<sub>20</sub>Al<sub>25</sub>, Dy<sub>55</sub>Co<sub>20</sub>Al<sub>24.5</sub>-B<sub>0.5</sub>, Dy<sub>55</sub>Co<sub>20</sub>Al<sub>24.5</sub>C<sub>0.5</sub>, Dy<sub>55</sub>Co<sub>20</sub>Al<sub>24.8</sub>N<sub>0.2</sub>, and Dy<sub>55</sub>Co<sub>20</sub>Al<sub>24.5</sub>r, are denoted as DyCoAl, DyB0.5, DyC0.5, DyN0.2, and DySi1, respectively. With a minor addition of metalloids, the GFA of Dy-based BMGs was enhanced significantly, as shown in Fig. 1b, accompanied by variations in thermal properties (Fig. S1 and Table S1). From our previous studies, the improvement in GFA can be attributed to the enhanced stability of the metallic melt and the fragile-to-strong transition of the supercooled liquid resulting from the distinct change in medium-range order [34,35]. The main objective of this work is to reveal the variation of structural/elastic heterogeneity on different length scales and relaxation behavior with a minor addition of metalloid elements.

The dynamic relaxation behaviors of the Dy-based BMGs were first investigated by DMA. The relaxation spectra of the temperature dependence of the storage (E') and loss moduli (E'') at 1 Hz are displayed in Fig. 2a for the five BMGs. The E" curves of all Dy-based BMGs exhibit pronounced β-relaxation shoulders around 400-550 K, followed by sharp a-relaxation peaks at ~650 K. Correspondingly, the E' curves present a shallow and deep minimum around the  $\beta$ - and  $\alpha$ -relaxation peaks of E''. The relaxation spectra at frequencies of 1, 2, 5, and 10 Hz were further collected. With increasing frequency, the  $\beta$ -relaxation shoulder moves to higher temperatures, as shown typically for the DySi1 BMG in Fig. 2b. The activation energy  $(E_{\beta})$  of  $\beta$ relaxation determined from the Arrhenius plots in Fig. 2c for the BMGs with different metalloids is plotted in Fig. 2d. An evident change in  $\textit{E}_{\beta}$  upon microalloying is found. To determine the obviousness of β-relaxation in the dynamical mechanical spectrum, the parameter  $\angle A$  defined in Ref. [36] was also determined and is shown in Fig. 2d. The angle  $\angle A$  increases with the addition of B, C, and N and decreases slightly with the addition of Si, indicating a similar alloying element dependence to  $E_{\beta}$ .

Because β-relaxation correlates well with structural/dynamical heterogeneities and defects, such as liquid-like regions, flow units, and shear transformation zones [4,20-24], we further examine the elastic and structural heterogeneities on different length scales (micrometer and nanometer scales) as well as stress-induced relaxation by the nanoindentation method, from which the relaxation spectra are recorded. Nanoindentation experiments at an array of  $14 \times 14$  sites were performed for each BMG sample to detect the variation of elastic heterogeneity upon minor addition (Fig. S2). Typical two-dimensiaonl (2D) maps of the reduced elastic moduli  $(E_r)$  of the DyCoAl and DySi1 BMGs are exhibited in Fig. 3a, b, showing a clear spatial fluctuation of the elastic properties. Some islands with low  $E_r$  are surrounded by a continuous zone with medium or high  $E_r$ . A typical distribution of the normalized  $E_r$  obtained from the 2D map of DyCoAl is displayed in Fig. 3c and the variation of the average  $E_{\rm r}$ with composition is shown in Fig. S3. The full width at halfmaxima (FWHMs) of the distribution curves are 4.3%, 1.7%, 4.8%, 3.5%, and 2.8% for the DyCoAl, DyB0.5, DyC0.5, DyN0.2, and DySi1 BMGs, respectively (Fig. 3d), showing an evident change in elastic heterogeneity. The addition of the C element increases the degree of elastic heterogeneity, but the addition of the other three elements decreases it. No clear correlation between the degree of heterogeneity on the micrometer scale (in terms of FWHM) and  $E_{\beta}$  (or  $\angle A$ ) is observed. This suggests that heterogeneity on a smaller length scale dominates the variation



**Figure 1** (a) Enthalpy of mixing ( $\Delta H_{mix}$ ), atomic radius ( $\varepsilon_i$ ), and electronegativity ( $\varphi_i$ ) for the studied Dy-based BMGs. (b) XRD patterns for the Dy-based BMG samples with the critical diameter.



**Figure 2** (a) Temperature dependence of the storage (*E'*) and loss moduli (*E''*) at a heating rate of 2 K min<sup>-1</sup> for the DyCoAl, DyB0.5, DyC0.5, DyN0.2, and DySi1 BMGs. (b) Evolution of *E''* with temperature at different driving frequencies for the DySi1 BMG. (c) Arrhenius plots of  $\ln f$  versus  $1000/T_{\beta}$  for the Dybased BMGs. (d) Activation energy of  $E_{\beta}$  and  $\angle A$  for the Dy-based BMGs.



**Figure 3** 2D maps of the  $E_r$  of the (a) DyCoAl and (b) DySi1 BMGs. (c) Distribution of  $E_r$  for the DyCoAl BMG. (d) FWHM of the  $E_r$  distributions of the Dy-based BMGs. (e) Relaxation spectrum of the DyCoAl BMG. The inset shows the typical creep curve. (f) Variation in the positions of the first and second peaks in the relaxation spectrum with composition.

of  $E_{\beta}$  and obviousness of relaxation, and it is possible that heterogeneity on the micrometer scale has a more complex influence on  $\beta$ -relaxation.

Then, the relaxation time spectra from the analysis of the anelastic part of creep were collected to further detect the variation of structure defects with different sizes. The Maxwell-Voigt model, including one Maxwell unit and two Kelvin units illustrated in Fig. S4, is used to describe creep deformation [37–40]. A typical creep curve under the indentation process and its fitting by the Maxwell-Voigt model is presented in the inset of Fig. 3e for the DyCoAl BMG. The anelastic part of the creep is analyzed considering the relaxation time spectrum, which can be determined from Refs. [38,39]:

$$L(\tau) = \left[\sum_{i=1}^{n} \left(1 + \frac{t}{\tau_i}\right) \frac{h_i}{\tau_i} e^{-\frac{t}{\tau_i}} \frac{A_0}{P_0 h_{\rm in}} t \Big|_{t=2\tau},$$
(1)

where *L* is the spectrum intensity, *t* is the holding time,  $h_i$  is the indentation depth, and  $\tau_i$  is the characteristic relaxation time of

the *i*-th anelastic Kelvin unit, *n* is equal to 2, and  $A_0/P_0$  is the inverse of hardness. From Fig. 3e, two separate relaxation peaks with characteristic relaxation times  $\tau_1$  and  $\tau_2$  are observed in the relaxation spectrum. It has been suggested that the first ( $\tau_1$ ) and second ( $\tau_2$ ) peaks are ascribed to activated defects with smaller and larger sizes, respectively [38,39]. From Fig. 3f,  $\tau_1$  and  $\tau_2$  show slightly different composition dependences, which may be associated with variation in the degree of heterogeneity. Fig. 3f further implies that microalloying changes the distribution of the size of activated defects during creep deformation: the addition of the B element tends to increase the size of the smaller activated defects (corresponding to  $\tau_1$ ) during creep deformation, but the addition of the N or C element tends to decrease it. The variation in defect distribution should influence  $\beta$ -relaxation, which remains elusive at present.

Subsequently, the local structure of BMG samples on atomic and nanometer scales was further characterized by TEM to determine the structural motif responsible for  $\beta$ -relaxation. Three representative HRTEM images of the DyCoAl, DyC0.5,

and DyN0.2 BMGs are presented in Fig. 4a-c, respectively, showing typical amorphous structures. Autocorrelation function (ACF) analysis was then conducted to determine the local structure orders on a scale of 1-2 nm [34,41,42]. The square region marked in the HRTEM image is divided into 100 segments, and the size of each cell is  $1.98 \text{ nm} \times 1.98 \text{ nm}$ . Note that ~2 nm is the typical length scale of the medium-range order of MGs [43]. The corresponding ACF arrays for the DyCoAl, DyC0.5, and DyN0.2 BMGs are shown in Fig. 4d-f, respectively, and those of the other two BMGs are shown in Figs S5 and S6. Some cells in the maps present clear fringe-like patterns, as marked by red squares, which are defined as medium-range imperfect order (IPO) or crystal-like order in some publications and are easy to distinguish from other regions with typical disordered structures (Fig. S7) [34]. The fraction of clusters with IPO  $(F_c)$  was thus calculated to explore the effect of microalloying on the local structure of BMGs. From Fig. 4d, the  $F_c$  of the DyCoAl BMG is 7.3% ± 0.5%. After microalloying the metalloid elements, more clusters with IPO can be observed, as shown in Fig. 4e and f. For instance, the F<sub>c</sub> of DyN0.2 BMG is 14.7%  $\pm$  0.9%, which is approximately twice larger than that of the DyCoAl BMG. Strikingly, the variation of  $F_c$  with the metalloids (Fig. 5a) resembles that of  $E_{\beta}$  (Fig. 2d), demonstrating that  $\beta$ -relaxation correlates well with the structural motif with

IPO. To shed light on the correlation between  $F_c$  and  $E_\beta$ , we analyzed the chemical influence on the  $\beta$ -relaxation and formation of clusters with IPO.  $\beta$ -relaxation is associated with the magnitude and fluctuations of chemical interactions [27]. The mean chemical affinity  $\Delta H_{\text{mix}}$  of the alloy system is then calculated by using the weighted average approach  $(\Delta H_{\text{mix}} = 4 \sum_{A \neq B} \Delta H_{AB}^{\text{mix}} c_A c_B)$  (where  $c_A$  and  $c_B$  are the molar percentages of elements A and B, respectively) [44] and is shown in Fig. 5a. It is evident that  $\Delta H_{\text{mix}}$  decreases after metalloid addition, especially for C, N, and Si. The variation of  $\Delta H_{\text{mix}}$  and  $F_{\rm c}$  upon metalloid addition indicates that a large  $-\Delta H_{\rm mix}$  may be beneficial for the formation of clusters with IPO. However,  $\Delta H_{\rm mix}$  cannot predict the accurate variation of  $E_{\beta}$  and  $F_{\rm c}$ . For instance, although the  $E_{\beta}$  and  $F_{c}$  values for the C, N, and Simicroalloying BMGs are different, their  $\Delta H_{\text{mix}}$  values are almost the same. In addition, we find that the distribution of chemical interactions cannot interpret the minor addition effect in these Dy-based BMGs showing pronounced  $\beta$ -relaxations either. For example, although the addition of B causes significant fluctuations in the enthalpy of mixing ( $\Delta H_{\rm AB}^{\rm mix})$  of the atomic pairs (Fig. 1), the DyB0.5 BMG shows increased  $\angle A$  of the  $\beta$ -relaxation. Accordingly, the distinctions of relaxation behaviors such as  $E_{\beta}$  and  $\angle A$  upon minor addition cannot be well demonstrated based only on the  $\Delta H_{\rm mix}$  and fluctuations of chemical interactions.

We further consider the intensity of interaction ( $W_{AB}$ ) defined (based on the Darken-Gurry theory) as  $W_{AB} = \left(\frac{\Delta \varepsilon_{AB}}{0.15}\right)^2 + \left(\frac{\Delta \varphi_{AB}}{0.4}\right)^2$ , where  $\Delta \varepsilon_{AB}$  is the difference in

atomic radius and  $\Delta \varphi_{AB}$  is the difference in electronegativity, reflecting the bonding nature between two atoms associated with the compound-forming tendency [45,46]. Here, the  $W_{AB}$  between Dy and the metalloid elements is calculated (Fig. 5a). For the DyCoAl BMG, the RE-containing clusters serve as the primary structural units, and the evaluated coordination number of the RE-Al pair in RE-TM (transition metal)-Al MGs is approximately 16 [47,48]. Thus, the  $W_{AB}$  between Dy and Al is utilized for comparison. Interestingly,  $W_{AB}$  shows the same variation trend with  $F_c$  (or  $E_\beta$ ) as metalloids are changed, although the slight difference in metalloid content is not considered in the definition of  $W_{AB}$ . Thus, the  $W_{AB}$  between the principal and microalloying elements can be considered as a simple parameter to characterize  $F_c$  for different microalloying



Figure 4 HRTEM images of the (a) DyCoAl, (b) DyC0.5, and (c) DyN0.2 BMG samples used in the DMA test. Corresponding autocorrelation segments of the selected square areas in (a-c) for the (d) DyCoAl, (e) DyC0.5, and (f) DyN0.2 BMGs.



**Figure 5** (a) Fraction of clusters with IPO ( $F_c$ ),  $\Delta H_{mixo}$  and intensity of interaction ( $W_{AB}$ ) between Dy and metalloids for the DyCoAl, DyB0.5, DyC0.5, DyN0.2, and DySi1 BMG samples. (b) Schematic illustration of the atomic structures of IPOs and liquid-like regions. The blue and purple balls are atoms in the solid-like and liquid-like regions, respectively, and the reddish-brown balls are clusters with IPO in the liquid-like regions.

systems. The effectiveness is due to the comprehensive consideration of the electronegative, atomic radius, and enthalpy of mixing in  $W_{AB}$ . Figs 5a and 2d illustrate that the correlation between  $\beta$ -relaxation and the clusters with IPO is associated with the interaction between the principal and microalloying elements.

A recent theoretical work correlates β-relaxation with the excitations of string-like configurations, where a group of atoms moves back and forth cooperatively and reversibly like a string [30]. Subsequent molecular dynamics simulations for a Lennard-Jones glass and a model MG have supported this mechanism [49]. By simulation on a microsecond time scale, it was found that the most probable time of string-like motions is accordant with the  $\beta$ -relaxation time [50]. The close relationship between  $F_{\rm c}$  and  $E_{\rm \beta}$  and  $\angle A$  observed here suggests that the excitation of string-like movement primarily takes place in these regions with IPO. This is reasonable because the regions with IPO have imperfect translational symmetry (with a higher degree of geometrical frustration) and comparable magnitudes of interactions among the constituting atoms, which are favorable for activating a cooperative string-like motion of the  $\beta$ -relaxation event. Instead, regions with large fluctuations between certain atomic pairs or with wholly disordered structures tend to break the cooperative and reversible string-like motions. Therefore, the increase in  $F_{c}$  after microalloying can promote the excitation of string-like motifs for β-relaxation, resulting in a more pronounced shoulder in the metalloid-doped BMGs. Then, we discuss why a larger  $F_c$  of the metalloid-doped BMG contributes to a higher  $E_{\beta}$ . Despite the presence of the IPO on the ~2 nm scale, the amorphous structure is retained, and typical nanocrystals are not observed. The limited growth of the clusters with IPO shows the presence of some stable pinning clusters (probably icosahedral-like) around them. These pinning clusters hinder the growth of clusters with IPO. A larger  $F_c$  refers to denser pinning clusters as well, which makes the activation of  $\beta$ relaxation more difficult and thus leads to a larger  $E_{\beta}$ . A similar mechanism works in the microalloying effect on the GFA of Cu-, Dy-, and Gd-based BMGs [34,35,51]. The improvement of the GFA of these BMGs with a minor addition of Si or Y was associated with an increasing fraction of clusters with IPO. It has been suggested that clusters with IPO cannot grow due to the pinning effect of the surrounding icosahedron-like clusters on the one hand and decreases the thermodynamic driving force for crystallization on the other hand [51]. Although other factors may affect the  $\beta$ -relaxation, this work confirms the significant effect of atomic defects with IPO on  $\beta$ -relaxation.

Finally, we emphasize that the medium-range IPO structure plays a critical role in the glass dynamics, nanocrystallization, glass formation, and deformation of MGs [52-56]. Such a role is similar to that of defects (i.e., some lattice points that deviate from the regular geometrical arrangement of the atoms) in influencing the properties of a crystalline solid. For instance, in MG liquids with an abnormal liquid-liquid transition, it was found that the MG prepared by high-temperature liquid has less IPO than that by low-temperature liquid [56]. In particular, in an Fe-based BMG with large plasticity, homogeneously dispersed clusters (1-1.5 nm) with IPO are observed, which are responsible for the start-and-stop mechanism of shear transformation zones [52]. In FeNi-based and Co-based BMGs, improved plasticity was found to correlate with improved structural heterogeneity with the formation of IPO structures [53,54]. Because the activation of the structural units (shear transformation zones) of plastic deformations correlates closely with  $\beta$ -relaxation in MGs [11], the above correlation between IPO structures and plasticity gives further evidence for IPO as the underlying structural origin of  $\beta$ -relaxation in MGs.

#### **CONCLUSIONS**

To sum up, we investigated the effect of microalloying ( $\leq 1$  at%) on  $\beta$ -relaxation and spatial heterogeneity on different length scales. A direct relationship between  $\beta$ -relaxation and the degree of heterogeneity on the micrometer scale (the FWHM of the  $E_r$ distributions) or the mean chemical affinity or fluctuations in the enthalpy of mixing was not observed. Instead, both the obviousness of the shoulder peak and activation energy for βrelaxation are well linked to the fraction of medium-range structures/defects with IPO and the intensity of interaction  $W_{AB}$ . This means that cooperative string-like excitations most probably occur in regions with IPO. Note that many experimental results suggest the mechanism of local arrangements in loosely packed regions for  $\beta$ -relaxation [20–22,57]. This implies that medium-range structures/defects with IPO contributing to the β-relaxation are relatively loose (due to the high geometric frustration) or in liquid-like regions to aid in cooperative stringlike movements (Fig. 5b). It was experimentally revealed by angstrom-beam electron diffraction and scanning TEM that the lower-density regions in a Zr-Cu-Al MG contained IPO [58]. In addition, a recent simulation study stated that string-like motions are produced in a relatively loose environment in the  $Al_{90}Sm_{10}$  MG with pronounced  $\beta$ -relaxation [59]. These studies corroborate our arguments that nanostructures with IPO in the liquid-like regions dominate  $\beta$ -relaxation in the Dv-based MGs. The mechanism schematized in Fig. 5b can explain why distinct β-relaxation behaviors with pronounced peaks, shoulders, and excess wings are observed in MGs, although they generally contain and may have a similar fraction of liquid-like regions. The key point lies in the fraction of medium-range structures/ defects with IPO (in favor of string-like motions) in the liquidlike regions. Therefore, this work provides new insights into the atomic-scale mechanism of  $\beta$ -relaxation in MGs.

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**Conflict of interest** The authors declare that they have no conflict of interest.

**Supplementary information** Supporting data are available in the online version of the paper.



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### 中程尺度类晶体结构决定非晶合金慢二次弛豫

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**摘要** 二次弛豫特别是慢β弛豫和结构不均匀性是非晶合金悬而未决 的关键问题. 尽管经历了几十年的深入研究, 慢β弛豫与结构不均匀性 之间的本征关联及其成分依赖性尚未建立. 本文以镝基块体非晶合金 为载体, 通过微量掺杂不同类金属元素包括硼、碳、氮和硅, 实现了β 弛豫的有效调控,并且揭示了其原子尺度结构起源. 通过对比研究混合 焓、弹性不均匀度、相互作用强度和不完美序结构(或类晶体结构)对 β弛豫的影响, 发现β弛豫强度与中程类晶体结构的含量密切相关(与混 合焓没有显著的对应关系), 这表明原子的链状协同运动发生在含有类 晶体结构的中程序软区. 此外, 镝元素和类金属元素之间的相互作用强 度对于类晶体结构的形成至关重要. 本工作对于理解β弛豫的原子结构 起源和调控非晶合金性能具有重要意义.